

GENETIC OPERATORS

In this exercise we study three genetic operators: **Selection, Crossover and Mutation**:

1. Read de basics of each operator
2. Classify each method into one of the 3 operators

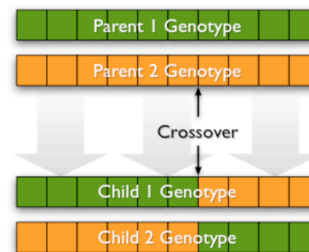
SELECTION OPERATOR

Decide which individuals will breed a new generation.

- The key idea is to give preference to better individuals, allowing them to pass on their genes to the next generation.
- The goodness of each individual depends on its fitness.
- Some individuals will be selected more than once, while others will die without leaving any descent.

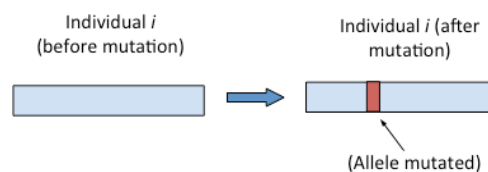
CROSSOVER OPERATOR

- Two individuals are chosen from the population using the selection operator.
- The two new offspring created from this mating are put into the next generation of the population.
- By recombining portions of good individuals, this process is likely to create even better individuals.



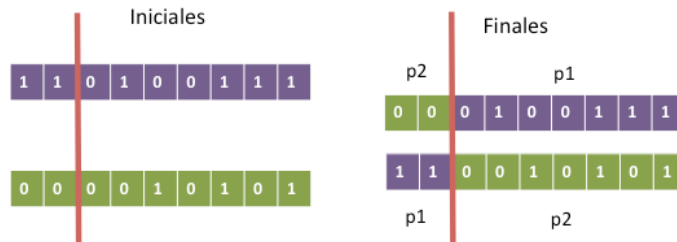
MUTATION OPERATOR

- Alter each gene independently with a probability p_m
- p_m is called the mutation rate
Typically between $1/\text{pop_size}$ and $1/\text{chromosome_length}$



METHOD 1: Choose a random point on the two parents

- Split parents at this point
- Create children by exchanging tails
- P_c typically in range (0.6, 0.9)



METHOD 2: Insertion

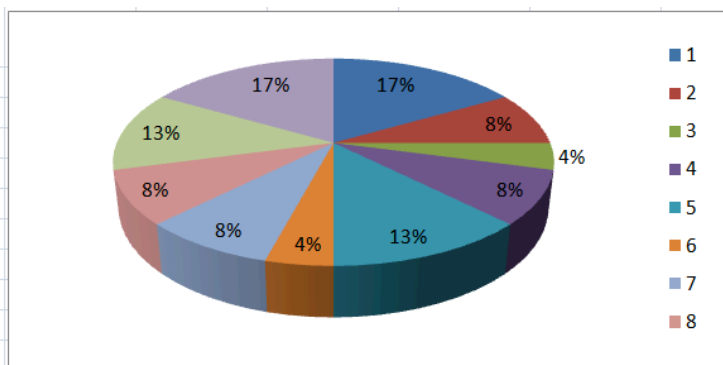
- Pick two allele values at random
- Place the first to follow the second, shifting the rest along to accommodate
- Note that this preserves most of the order and the adjacency information

$$v = (1\ 9\ \mathbf{8}\ 7\ 6\ 5\ \mathbf{4}\ 3\ 2) \quad v' = (1\ 9\ 7\ 6\ 5\ \mathbf{8}\ 4\ 3\ 2)$$

METHOD 3 – Roulette Wheel

- Assign to each individual a part of the roulette wheel, based on the evaluation function
- Spin the wheel n times to select n individuals

Función de Evaluación	Prob	Acumulada
4	0,17	0,17
2	0,08	0,25
1	0,04	0,29
2	0,08	0,38
3	0,13	0,50
1	0,04	0,54
2	0,08	0,63
2	0,08	0,71
3	0,13	0,83
4	0,17	1,00



METHOD 4: Inversion

Invert the order of a sub-chain

$$v = (1\ 9\ 8\ | \ \mathbf{7\ 6\ 5\ 4}\ | \ 3\ 2) \quad v' = (1\ 9\ 8\ | \ \mathbf{4\ 5\ 6\ 7}\ | \ 3\ 2)$$

METHOD 5: Tournament

- Pick k members at random, then select the best of these

- Repeat to select more individuals

METHOD 6: Bit Flip (Binary)

We select one or more random bits and flip them (from 0 to 1 or viceversa)

METHOD 7: PMX

1. Two points are selected at random (or determined before execution)

$$p_1 = (1\ 2\ 3\ | 4\ 5\ 6\ 7\ | 8\ 9) \quad p_2 = (4\ 5\ 2\ | 1\ 8\ 7\ 6\ | 9\ 3)$$

2. The central part of one parent is mapped to the central area of the other parent:

$$s_1 = (x\ x\ x\ | 1\ 8\ 7\ 6\ | x\ x) \\ s_2 = (x\ x\ x\ | 4\ 5\ 6\ 7\ | x\ x)$$

taking into account the interchanges: 1/4, 8/5, 7/6, y 6/7

2. Then, the values that are not in conflict (already inserted) are added to each offspring:

For example value 1 in p1 already exists in s1, then we look for the next value

$$p_1 = (1\ 2\ 3\ | 4\ 5\ 6\ 7\ | 8\ 9) \quad s_1 = (x\ 2\ 3\ | 1\ 8\ 7\ 6\ | x\ 9) \\ p_2 = (4\ 5\ 2\ | 1\ 8\ 7\ 6\ | 9\ 3) \quad s_2 = (x\ x\ 2\ | 4\ 5\ 6\ 7\ | 9\ 3)$$

3. Finally, the values in conflict must be replaced by the interchanges: 1/4, 8/5, 7/6, y 6/7

For example value 1 in p1 already exists in s1, the interchange was 1/4, thus, value 4 is added instead

$$s_1 = (4\ 2\ 3\ | 1\ 8\ 7\ 6\ | 5\ 9) \\ s_2 = (1\ 8\ 2\ | 4\ 5\ 6\ 7\ | 9\ 3)$$

METHOD 8: OX

From a substring of p1, and preserving the relative order of the p2:

1. Two points are selected at random (or determined before execution)

$$p_1 = (1\ 2\ 3\ | 4\ 5\ 6\ 7\ | 8\ 9) \quad p_2 = (4\ 5\ 2\ | 1\ 8\ 7\ 6\ | 9\ 3)$$

2. The central part is copied into the offspring:

$$s_1 = (x\ x\ x\ | 4\ 5\ 6\ 7\ | x\ x) \quad s_2 = (x\ x\ x\ | 1\ 8\ 7\ 6\ | x\ x)$$

3. Starting from the second point, copy the values of the other parent in the same order, omitting those repeated values.

$$s_1 = (x\ x\ x\ | 4\ 5\ 6\ 7\ | 9\ 3) \quad s_2 = (x\ x\ x\ | 1\ 8\ 7\ 6\ | 9\ 2)$$

4. When the end of the string is reached, start from the first position on the left:

$$s_1 = (2\ 1\ 8\ | 4\ 5\ 6\ 7\ | 9\ 3) \quad s_2 = (3\ 4\ 5\ | 1\ 8\ 7\ 6\ | 9\ 2)$$

METHOD 9: Swap

We select two positions on the chromosome at random, and interchange the values. (This is common in permutation-based encodings).

EXERCISES

Use the following random numbers:

8	2	1	3	6	2	3	8	4	5	7	0.5129	0.3693	0.4460	0.3933	0.1194
6	1	3	8	4	7	3	6	4	4	2	0.9404	0.3204	0.4032	0.4605	0.0336
6	5	3	1	5	1	5	6	1	5	8	0.5083	0.8044	0.6344	0.4156	0.6579
1	8	7	7	4	6	2	4	2	7	2	0.8024	0.3504	0.1922	0.5281	0.0111
											0.8624	0.2720	0.0018	0.8621	0.0950
											0.4714	0.5729	0.2331	0.1582	0.9280
											0.6290	0.1438			

- Given the following individuals belonging to the 4-Queens problem, where the fifth column corresponds to the evaluation function, apply all the selection operators studied above:

```

2 1 3 4 4
1 3 2 4 4
3 4 1 2 2
3 2 4 1 5
4 2 3 1 4
2 3 4 1 2
4 3 1 2 4
1 4 2 3 5
  
```

- Apply the crossover methods according to the representation of the individuals. Crossover points are 3 and 7:

A)

```

6 3 7 8 5 1 2 4 9 10
2 10 8 9 1 5 7 6 3 4
  
```

B)

```

0011100011
1111010101
  
```

- Apply mutation operators when possible, according to the representation. PMut=0.2

A)

```

00011100011
  
```

B)

```

6 10 7 8 5 1 2 4 9 3
  
```